# Planetary migration: basics, recent results and new challenges

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Nustration: planet in a protoplanetary disk (numerical simulation)

# **Exoplanets statistical properties**

#### 473 exoplanets to date



# **Connection with planetary formation**





Hot Jupiters should have formed further out and migrated inward



# **Connection with planetary formation**



Possible fast formation far through gravitational instability, but what about migration?



# What do we know about protoplanetary disks?



Millimeter interferometry (e.g. CO emission lines) gives insight into disk properties beyond ~ 50 AU, *a priori* far from regions of planet formation (1-10AU)

Surface density and temperature are modelled as power-law functions of radius,  $\Sigma \sim r^{-1.5}$ , T ~ r^{-0.5}

In (the inner) regions of planet formation, disks should be **optically thick**, and their self-gravity should be negligible

**Disk turbulence** in these regions? generally modelled by viscous diffusion.

# Disk response to an embedded protoplanet

(see animation)

# Disk response to an embedded protoplanet



The planet excites a one-armed spiral wake propagating both inwards and outwards.

The gravitational force that the wake exerts onto the planet modifies the <u>planet's semi-</u><u>major axis</u>, eccentricity and inclination.

**Planetary migration** 

# Disk response to an embedded protoplanet

The inner wake exerts a **positive torque** on the planet, and tends to impose an **outward migration** 

The outer wake exerts a negative torque on the planet, and tends to impose an inward migration



The sum of these two torques, called the differential Lindblad torque, is negative  $\rightarrow$  inward migration (Ward 1986)



# **Differential Lindblad torque: resonances**



# **Differential Lindblad torque**

Can we reverse the sign of the Lindblad torque with a steeper surface density profile ?



Now assume a steeper surface density profile...

# **Differential Lindblad torque**

Can we reverse the sign of the Lindblad torque with a steeper surface density profile ?



 $\rightarrow$  No, the Lindblad torque is insensitive to the density gradient

Ward 1997

# **Differential Lindblad torque**

But, the Lindblad torque may be reduced or even reversed in a super-Keplerian disk, e.g.: Hasegawa & Pudritz 2010



# Type I migration in a nutshell



The planet exchanges angular momentum with:

- circulating fluid elements:
  - $\rightarrow$  differential Lindblad torque
- librating fluid elements:



# Type I migration in a nutshell



The planet exchanges angular momentum with:

- circulating fluid elements:

 - librating fluid elements:
 → corotation torque (horseshoe drag)

# Type I migration in a nutshell



# Saturation of the corotation torque

#### Vortensity is advected in 2D inviscid barotropic flows



In such flows, the horseshoe drag ultimately **vanishes** (saturates) as vortensity is progressively stirred up in the horseshoe region

## Desaturating the corotation torque

**Viscosity** (disk is **laminar**,  $\mathbf{v} = \alpha c H$ ) diffuses vortensity inside of the horseshoe region, and can maintain the corotation torque to its (maximum) fully unsaturated value...



Masset (2002)

# Desaturating the corotation torque



## Enhancing the corotation torque: the planet trap



## Enhancing the corotation torque in radiatively inefficient disks

Inclusion of the gas thermodynamics:

Paardekooper & Mellema (2006) - 3D + radiative transfer



# Enhancing the corotation torque in radiatively inefficient disks

# Additional component of the horseshoe drag, scaling with the entropy gradient

Baruteau & Masset (2008a), Paardekooper & Papaloizou (2008), Masset & Casoli (2009), Paardekooper, Baruteau, Crida & Kley (2009)



This boost of the corotation torque may **solve** the lingering problem of a "too fast" type I planetary migration

# A torque formula for population synthesis models

This boost of the corotation torque may **solve** the lingering problem of a "too fast" type I planetary migration

- depending on the entropy (density+temperature) gradient
- depending on the magnitude of the diffusion processes (viscosity + thermal diffusion)

# A torque formula for population synthesis models

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# $\rightarrow$ need for a torque formula to be used by population synthesis models



# A torque formula for population synthesis models

This boost of the corotation torque may **solve** the lingering problem of a "too fast" type I planetary migration

- depending on the entropy (density+temperature) gradient
- depending on the magnitude of the <u>diffusion</u> processes (viscosity + thermal diffusion)



→ what happens in a *turbulent* disk?

# Corotation torque in turbulent disks



**Context** 3D MHD calculations... coming soon!

#### Aim

desaturation of the corotation torque with turbulence

#### **Methods**

2D Hydro + stochastic forcing (turbulent potential, Laughlin et al. 2004)

The parameters of the « turbulent potential » are **tuned** to give turbulence statistical properties as close as possible to those of 3D MHD runs

# Comparison with laminar disk models



These results suggest that the desaturation properties of the corotation torque in turbulent disk models agree with those of laminar disk models

# What about in MRI simulations?



# Summary on type I migration



. . . .

The torque driving the migration of low-mass planets is two-fold:



To do list: - interplay with MHD turbulence (e.g. dead zone and planet trap), including several planets
- 3D torque formula for type I migration in radiative disks

# Larger planet masses: the planet migration zoo



#### Courtesy of F. Masset

# Thank you for your attention!